

Units and Measurements

Example Problem

A laboratory experiment measures the boiling point of water. The accepted value of the boiling point of water at standard atmospheric pressure is 100°C . The measured boiling point in the experiment is 98°C . Calculate the percentage error.

Solution:

1. **Determine the true value:** 100°C .
2. **Measure the quantity:** 98°C .
3. **Calculate the absolute error:**
Absolute Error = $|98 - 100| = 2^{\circ}\text{C}$
4. **Calculate the percentage error:**
Percentage Error = $(\frac{2}{100}) \times 100\% = 2\%$

Similar Problems

1. A student measures the length of a table as 1.95 meters, but the actual length is 2 meters. Calculate the percentage error.
2. The true mass of a gold bar is 500 grams. A jeweler measures it and finds it to be 495 grams. Calculate the percentage error.
3. During an experiment, the density of a substance is measured as 8.1 g/cm^3 , but the true density is known to be 8.0 g/cm^3 . Calculate the percentage error.
4. A thermometer shows the temperature as 25.5°C , while the actual temperature is 26.0°C . Calculate the percentage error.
5. The actual speed of a car is 60 km/h, but a speedometer reads it as 58 km/h. Calculate the percentage error.
6. An electronic scale shows the weight of an object as 150 grams, but the true weight is 155 grams. Calculate the percentage error.

Key

1. **Problem 1:**
Absolute Error = $|1.95 - 2| = 0.05 \text{ meters}$
Percentage Error = $(\frac{0.05}{2}) \times 100\% = 2.5\%$

2. Problem 2:

$$\text{Absolute Error} = |495 - 500| = 5 \text{ grams}$$

$$\text{Percentage Error} = \left(\frac{5}{500}\right) \times 100\% = 1\%$$

3. Problem 3:

$$\text{Absolute Error} = |8.1 - 8.0| = 0.1 \text{ g/cm}^3$$

$$\text{Percentage Error} = \left(\frac{0.1}{8.0}\right) \times 100\% = 1.25\%$$

4. Problem 4:

$$\text{Absolute Error} = |25.5 - 26.0| = 0.5^\circ\text{C}$$

$$\text{Percentage Error} = \left(\frac{0.5}{26.0}\right) \times 100\% \approx 1.92\%$$

5. Problem 5:

$$\text{Absolute Error} = |58 - 60| = 2 \text{ km/h}$$

$$\text{Percentage Error} = \left(\frac{2}{60}\right) \times 100\% \approx 3.33\%$$

6. Problem 6:

$$\text{Absolute Error} = |150 - 155| = 5 \text{ grams}$$

$$\text{Percentage Error} = \left(\frac{5}{155}\right) \times 100\% \approx 3.23\%$$