



INTEGRALS SIMPLE AND SUBSTITUTION METHODS

Class 12 - Mathematics

Time Allowed: 1 hour and 30 minutes

Maximum Marks: 45

1. Find: $\int \frac{dx}{9+4x^2}$ [1]
2. Find: $\int \frac{x^3+1}{x^3-x} dx$ [1]
3. Find $\int xe^{(1+x^2)} dx$ [1]
4. Find: $\int e^{2\log x} dx$ [1]
5. Find: $\int \frac{\sin x}{\sin^3 x + \cos^3 x} dx$ [3]
6. Evaluate: $\int \frac{2x}{(2x+1)^2} dx$. [3]
7. Evaluate: $\int \frac{x}{\sqrt{x+a} + \sqrt{x+b}} dx$ [3]
8. If $f(x) = x + b$, $f(1) = 5$, $f(2) = 13$, find $f(x)$. [3]
9. If $f(x) = a \sin x + b \cos x$ and $f(0) = 4$, $f(\frac{\pi}{2}) = 3$, $f(\frac{\pi}{2}) = 5$, find $f(x)$. [5]
10. Integrate the function: $\frac{e^{\tan^{-1} x}}{1+x^2}$ [1]
11. Evaluate: $\int \operatorname{cosec} x dx$ [1]
12. Evaluate the integral: $\int \sin x \cos x dx$ [1]
13. Write a value of $\int \tan^3 x \sec^2 x dx$ [1]
14. Evaluate: $\int \frac{1+\sin x}{\sqrt{x-\cos x}} dx$ [1]
15. Evaluate: $\int \frac{x}{\sqrt{x+z}\sqrt{x-z}} dx$ [3]
16. Evaluate: $\int \frac{1}{\sin x(3+2\cos x)} dx$. [3]
17. Evaluate: $\int \frac{1}{p+q \tan x} dx$ [3]
18. Evaluate: $\int \frac{\sqrt{x^2+1}(\log|x^2+1|-2\log|x|)}{x^4} dx$. [5]
19. Evaluate: $\int \frac{x+\sqrt{x+1}}{x+2} dx$ [5]