

## Worksheets

Name

### Continuity and Differentiability

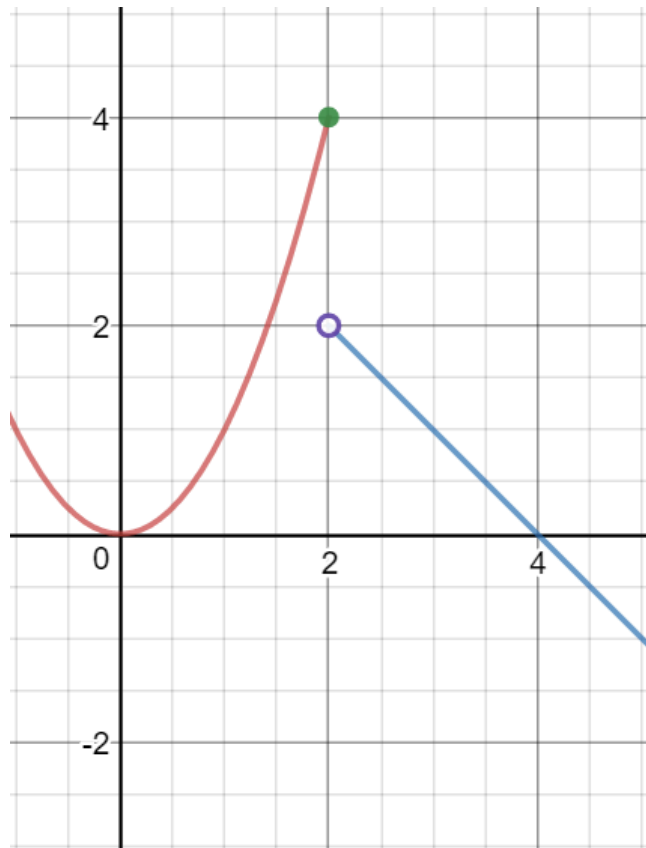
Total questions: 26

Worksheet time: 30mins

Instructor name: Stanley Walerski

Class

Date



1.

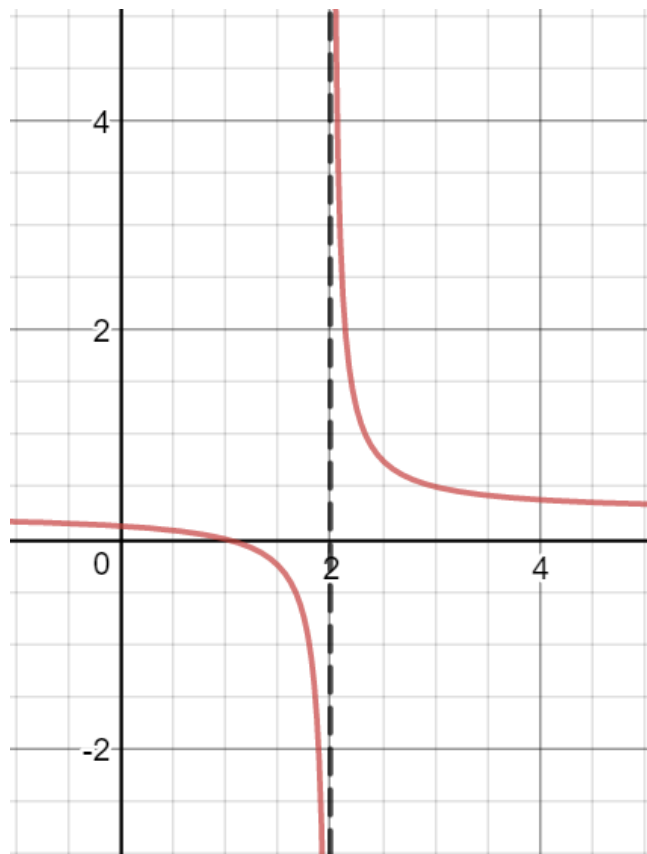
Name the discontinuity at  $x=2$ .

a) Continuous at  $x=2$

b) Jump Discontinuity

c) Removable Discontinuity

d) Infinite Discontinuity



2.

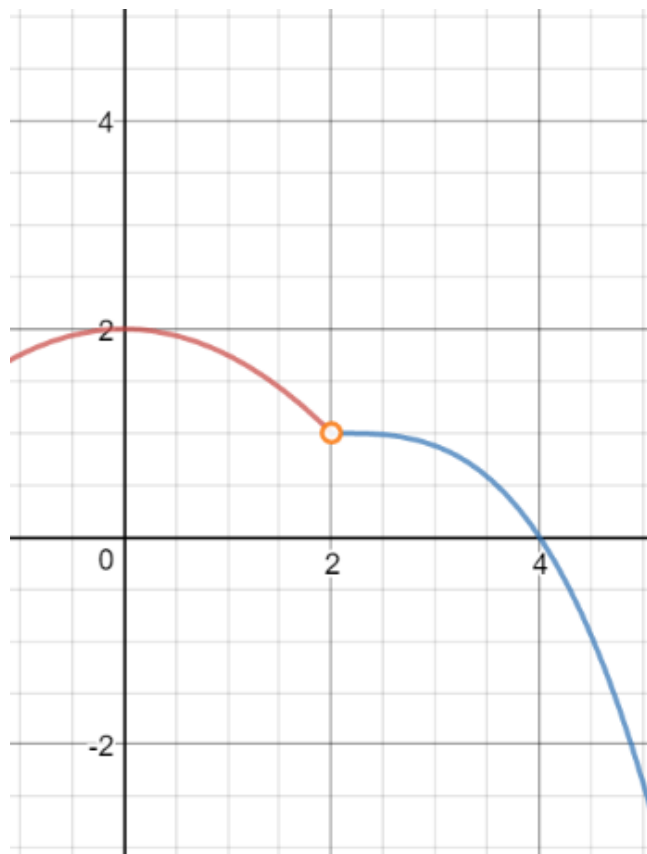
Name the discontinuity at  $x=2$ .

a) Jump Discontinuity

b) Removable Discontinuity

c) Continuous at  $x=2$

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3.

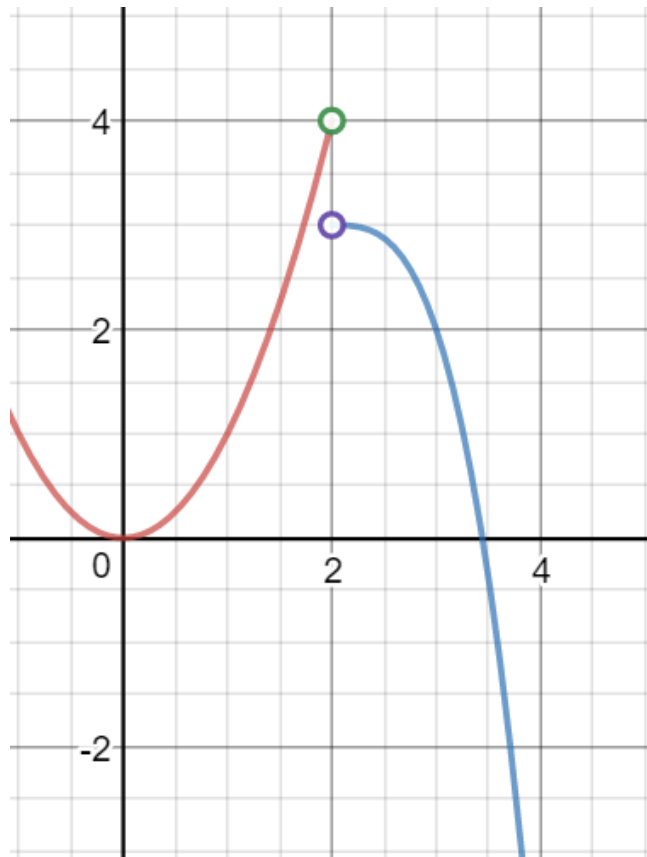
Name the discontinuity at  $x=2$ .

a) Jump Discontinuity

b) Removable Discontinuity

c) Continuous at  $x=2$

d) Infinite Discontinuity



4.

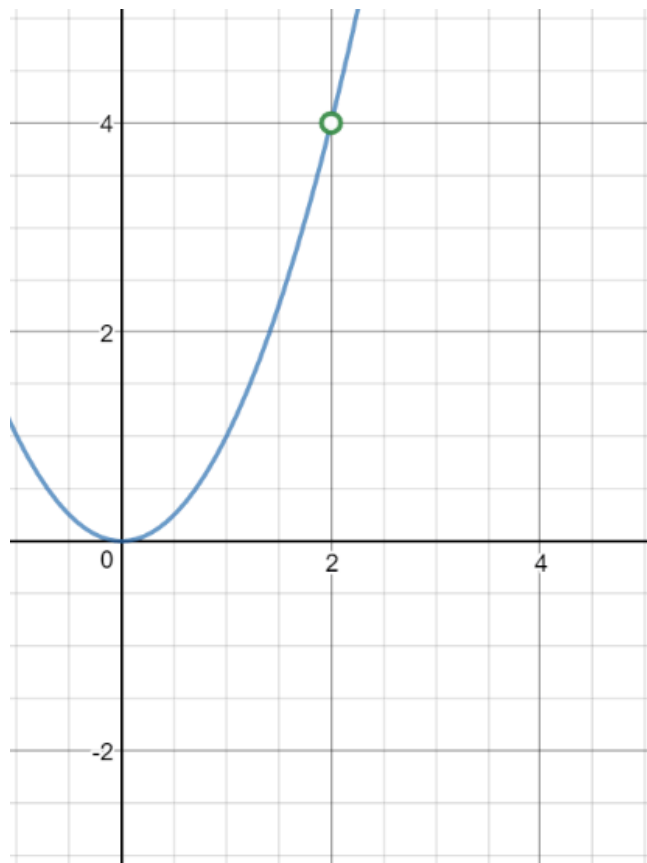
Name the discontinuity at  $x=2$ .

a) Infinite Discontinuity

b) Continuous at  $x=2$

c) Jump Discontinuity

d) Removable Discontinuity



5.

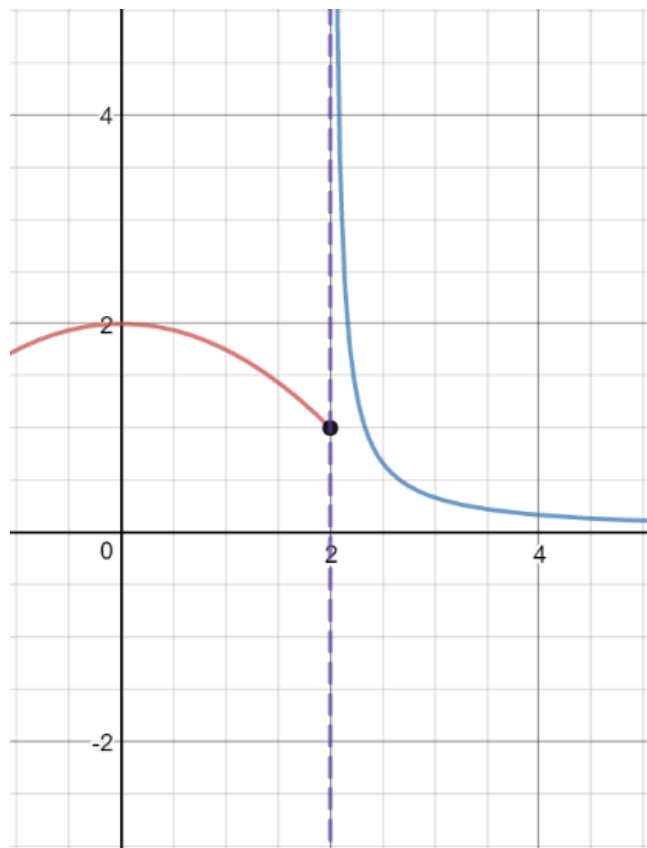
Name the discontinuity at  $x=2$ .

a) Continuous at  $x=2$

b) Infinite Discontinuity

c) Jump Discontinuity

d) Removable Discontinuity



6.

Name the discontinuity at  $x=2$ .

a) Removable Discontinuity

b) Jump Discontinuity

c) Continuous at  $x=2$

d) Infinite Discontinuity

7. Identify the point(s) of discontinuity.

$$f(x) = \frac{4}{x - 6}$$

a)  $x = 0$

b)  $x = 6$

c)  $x = 4$

d)  $x = -6$

8. Identify the point(s) of discontinuity.

$$f(x) = \frac{x - 1}{3x^2 - 3}$$

a)  $x = -1$  and  $x = 1$

b) Only  $x = 1$

c) Only  $x = -1$

d)  $x = 1$  and  $x = 3$

e) Only  $x = 3$

9. Determine any point(s) of discontinuity for the following function.

$$f(x) = \frac{3x - 6}{x^2 - 9x + 14}$$

a)  $x = 2$

b)  $x = 0$

c)  $x = 2$  and  $x = 7$

d) None

e)  $x = 7$

$$f(x) = \frac{x^2 + 7x + 10}{x^2 + 4x - 5}$$

10.

Identify the type of location of the discontinuity/discontinuities.

a) Removable at  $x = -5$ ; Infinite at  $x = 1$     b) Removable at  $x = 5$ ; Infinite at  $x = -1$

c) Removable at  $x = -5$ ; Jump at  $x = 1$     d) Infinite at  $x = 1$  and  $x = -5$

$$h(x) = \frac{x + 4}{x^2 - 2x - 35}$$

11.

Which of the following best describes the continuity at  $x = 5$ ?

- a) Jump Discontinuity at  $x = 5$       b) Removable Discontinuity at  $x = 5$   
c) Continuous at  $x = 5$       d) Infinite Discontinuity at  $x = 5$

$$f(x) = \frac{x^2 - 2x - 15}{x - 5}$$

12.

Which of the following best describes the continuity at  $x = 5$ ?

- a) Continuous      b) Jump Discontinuity at  $x = 5$   
c) Removable Discontinuity at  $x = 5$       d) Infinite Discontinuity at  $x = 5$

13. What is the domain of the function?  $v(t) = \frac{\sqrt{t+1}}{t-2}$

- a)  $t > -1, t \neq 2$       b)  $t \geq -1, t \neq 2$   
c)  $t > 2, t \neq -1$       d)  $t < 1$

14. Determine the domain:

$$g(x) = \sqrt{15 + 5x}$$

a)  $x \geq 3$

b)  $x > 3$

c)  $x > -3$

d)  $x \geq -3$

15. Determine the domain:

$$g(x) = \sqrt{x^2 + x - 20}$$

a)  $x \leq -5$  or  $x \geq 4$

b)  $x \leq -4$  or  $x \geq 5$

c)  $-4 \leq x \leq 5$

d)  $-5 \leq x \leq 4$

16. For a function,

$f(x)$  to be continuous at a point  $x = c$ , which of the following conditions must be met:

i.  $\lim_{x \rightarrow c} f(x)$  must exist

ii.  $f(c)$  must be defined

iii.  $\lim_{x \rightarrow c} f(x) = f(c)$

a) i and ii only

b) i only

c) iii only

d) i, ii, and iii

17. Can a function be continuous but not differentiable?

a) Yes

b) No

18. If a function is differentiable, it is also continuous.

a) It all depends on the function in question. b) Yes

c) No

19. If a function is differentiable at  $x=c$ , can it be discontinuous at  $x=c$ ?

a) It all depends on the function in question. b) Yes

c) No

20.

$$f(x) = \begin{cases} x^2 - 11x + 8, & x < 3 \\ -5x - 1, & x \geq 3 \end{cases}$$

Is the function continuous, differentiable, both, or neither at the rule change?

a) continuous

b) differentiable

c) neither

d) both





## Answer Keys

- |  |                                  |  |
|--|----------------------------------|--|
| 1. b) Jump<br>Discontinuity                        | 2. d) Infinite<br>Discontinuity  | 3. b) Removable<br>Discontinuity             |
| 4. c) Jump<br>Discontinuity                        | 5. d) Removable<br>Discontinuity | 6. d) Infinite<br>Discontinuity              |
| 7. b) $x = 6$                                      | 8. a) $x = -1$ and $x = 1$       | 9. a) $x = 2$                                |
| 10. a) Removable at $x = -5$ ; Infinite at $x = 1$ | 11. c) Continuous at $x = 5$     | 12. c) Removable<br>Discontinuity at $x = 5$ |
| 13. b) $t \geq -1, t \neq 2$                       | 14. d) $x \geq -3$               | 15. d) $-5 \leq x \leq 4$                    |
| 16. d) i, ii, and iii                              | 17. a) Yes                       | 18. b) Yes                                   |
| 19. c) No  | 20. d) both                      | 21. a) both                                  |
| 22. c) both  | 23. b) continuous                | 24. c) neither                               |
| 25. a) neither                                     | 26. d) continuous                |  |

