



Topic Tree for "Application of Derivatives" (Chapter 7)

1. Introduction to Differential Calculus

- Historical Background and Developments
- Objectives and Applications in Various Fields

2. Basic Concepts in Differentiation

- Definition of Derivative
- Notations and Interpretations of Derivatives
- Derivative as Slope and Rate of Change

3. Applications of Derivatives

- Increasing and Decreasing Functions
- Tangents and Normals to Curves
- Optimization Problems
- Related Rates of Change

4. Mean Value Theorem (MVT)

- Statement of MVT
- Geometric Interpretation
- Applications of MVT in Real-life Scenarios

5. Applications of the First Derivative

- Monotonicity and Critical Points
- Finding Extrema (Maxima and Minima)
- Use of First Derivative in Analyzing Functions

6. Applications of the Second Derivative

- Concavity and Points of Inflection
- Second Derivative Test for Local Extrema
- Curve Sketching Using Derivatives

7. L'Hôpital's Rule

- Indeterminate Forms ($0/0$ and ∞/∞)
- Application of L'Hôpital's Rule to Solve Limits

8. Optimization in Practical Problems

- Optimization in Geometry (Shapes and Areas)
- Business and Economics Applications
- Optimization in Physics and Engineering

9. Related Rates

- Problems Involving Two or More Variables Changing Over Time
- Techniques for Solving Related Rates Problems

10. Taylor and Maclaurin Series

- Introduction to Series Expansions
- Applications of Taylor and Maclaurin Series in Approximations

11. Summary and Exercises

- Chapter Summary and Key Formulas
- Practice Exercises with Solutions for Reinforcement