

Set Theory Basics Guide

Difference between Subset and Proper Subset:

- **Subset (\subseteq):** Set A is a subset of set B if every element of A is also an element of B. A set is always a subset of itself.
- **Proper Subset (\subset):** Set A is a proper subset of set B if every element of A is also an element of B, and B contains at least one element not in A. A set is not a proper subset of itself.

Examples of Subset:

1. $A = \{1, 2\}, B = \{1, 2, 3\} \rightarrow A \subseteq B$
2. $C = \{a, b\}, D = \{a, b, c, d\} \rightarrow C \subseteq D$
3. $E = \{x, y\}, F = \{w, x, y, z\} \rightarrow E \subseteq F$

Examples of Proper Subset:

1. $G = \{1, 2\}, H = \{1, 2, 3\} \rightarrow G \subset H$
2. $I = \{a\}, J = \{a, b, c\} \rightarrow I \subset J$
3. $K = \{m, n\}, L = \{m, n, o, p\} \rightarrow K \subset L$

Problems to Identify Subset and Proper Subset:

1. Identify whether $\{2, 4\}$ is a subset or proper subset of $\{2, 4, 6\}$.
2. Determine if $\{a, c\}$ is a subset or proper subset of $\{a, b, c, d\}$.
3. Check if $\{x, y\}$ is a subset or proper subset of $\{w, x, y, z\}$.
4. Assess whether $\{1, 3, 5\}$ is a subset or proper subset of $\{1, 2, 3, 4, 5\}$.
5. Evaluate if $\{p, q\}$ is a subset or proper subset of $\{p, q, r\}$.
6. Decide if $\{7, 8\}$ is a subset or proper subset of $\{6, 7, 8, 9\}$.
7. Verify whether $\{u, v, w\}$ is a subset or proper subset of $\{u, v, w, x\}$.
8. Judge if $\{3, 5, 7\}$ is a subset or proper subset of $\{3, 4, 5, 6, 7, 8\}$.
9. Confirm if $\{d, e\}$ is a subset or proper subset of $\{c, d, e, f\}$.
10. Determine whether $\{x, y, z\}$ is a subset or proper subset of $\{x, y, z\}$.

Key:

1. Proper Subset
2. Proper Subset
3. Proper Subset
4. Proper Subset
5. Proper Subset
6. Proper Subset
7. Proper Subset
8. Proper Subset
9. Proper Subset
10. Subset