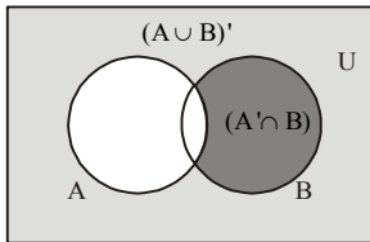


1. (c)  $\{5\}$  is a subset of A as  $5 \in A$   
 But,  $\{1, 2\}$  is not a subset of A as elements  $1, 2 \notin A$ .
2. (a) Let U be the set of consumers questioned X, the set of consumers who liked the product A and Y, the set of consumers who liked the product B. Then  $n(U) = 1000$ ,  $n(X) = 720$ ,  $n(Y) = 450$   
 $n(X \cup Y) = n(X) + n(Y) - n(X \cap Y) = 1170 - n(X \cap Y)$   
 $\therefore n(X \cap Y) = 1170 - n(X \cup Y)$   
 Clearly  $n(X \cap Y)$  is least  
 When  $n(X \cup Y)$  is maximum.  
 Now,  $X \cup Y \subset U$   
 $\therefore n(X \cup Y) \leq n(U) = 1000$   
 $\therefore$  the maximum value of  $n(X \cup Y)$  is 1000.  
 Thus the least value of  $n(X \cap Y)$  is 170
3. (d) For a set S, the partition of S is a set of subsets of S, such that they are pair-wise disjoint and their union is S.  
 In the options (a) & (b), the subsets are not disjoint.  
 In the option (c), the subsets are disjoint but their union is not equal to the given set.  
 Only the option (d) meets with both the requirements.
4. (a) From Venn-Euler's Diagram.

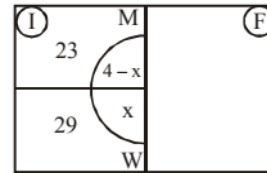


$$\therefore (A \cup B)' \cup (A \cap B) = A'$$

5. (d)  $A = \{(n, 2n) : n \in \mathbb{N}\}$  and  $B = \{(2n, 3n) : n \in \mathbb{N}\}$   
 Listing few members of each set  
 $A = \{(1, 2), (2, 4), (3, 6), \dots\}$   
 $B = \{(2, 3), (4, 6), (6, 9), \dots\}$   
 There is no member common to both these sets, hence.  
 $A \cap B = \phi$
6. (a)  $b\mathbb{N} = \{bx : x \in \mathbb{N}\}$   
 $c\mathbb{N} = \{cx : x \in \mathbb{N}\}$   
 $\therefore b\mathbb{N} \cap c\mathbb{N} = \{x : x \text{ is multiple of } b \text{ and } c \text{ both}\}$   
 $= \{x : x \text{ is multiple of l.c.m. of } b \text{ and } c\}$   
 $= \{x : x \text{ is multiple of } bc\}$   
 [given  $b$  and  $c$  are relatively prime  $\therefore$  l.c.m. of  $b$  and  $c = bc$ ]  
 $\therefore b\mathbb{N} \cap c\mathbb{N} = \{bcx : x \in \mathbb{N}\} = d\mathbb{N}$  (Given)  
 $\therefore d = bc$ .
7. (d)  $n(M) = 23, n(P) = 24, n(C) = 19$   
 $n(M \cap P) = 12, n(M \cap C) = 9, n(P \cap C) = 7$   
 $n(M \cap P \cap C) = 4$   
 We have to find  $n(M \cap P' \cap C'), n(P \cap M' \cap C'),$   
 $n(C \cap M' \cap P')$

$$\begin{aligned} \text{Now } n(M \cap P' \cap C') &= n[M \cap (P \cup C)'] \\ &= n(M) - n[(M \cap (P \cup C))] \\ &= n(M) - n[(M \cap P) \cup (M \cap C)] \\ &= n(M) - n(M \cap P) - n(M \cap C) + n(M \cap P \cap C) \\ &= 23 - 12 - 9 + 4 = 27 - 21 = 6 \\ n(P \cap M' \cap C') &= n[P \cap (M \cup C)'] \\ &= n(P) - n[P \cap (M \cup C)] \\ &= n(P) - n[(P \cap M) \cup (P \cap C)] \\ &= n(P) - n(P \cap M) - n(P \cap C) + n(P \cap M \cap C) \\ &= 24 - 12 - 7 + 4 = 9 \\ n(C \cap M' \cap P') &= n(C) - n(C \cap P) - n(C \cap M) + n(C \cap P \cap M) \\ &= 19 - 7 - 9 + 4 = 23 - 16 = 7 \end{aligned}$$

8. (c) We have  
 $\min n(A \cup B) = \max \{n(A), n(B)\} = \max \{3, 6\} = 6$   
 $\max n(A \cup B) = n(A) + n(B) = 9$   
 $\therefore 6 \leq n(A \cup B) \leq 9$
9. (b)  $A \Delta B = (A - B) \cup (B - A)$   
 $= \{1, 2\} \cup \{3, 4, 9\}$   
 $= \{1, 2, 3, 4, 9\}$
10. (a) See the following Venn diagram



$$\begin{aligned} n(I) &= 29 + 23 = 52 \\ n(F) &= 100 - 52 = 48 \\ n(M \cup D) &= n(M) + n(D) - n(M \cap D) \\ 24 &= 23 + 4 - n(M \cap D) \\ \therefore n(M \cap D) &= 3 \\ \therefore n(W \cap D) &= 4 - 3 = 1 \end{aligned}$$

11. (c) Suppose  $a \in X$  and  $a \in A$   
 $\Rightarrow a \in X \cup A \Rightarrow a \in Y \cup A$   
 $\Rightarrow a \in Y$  and  $a \in A$  ( $\because X \cup A = Y \cup A$ )  
 $\Rightarrow a \in Y \cap A \Rightarrow Y \cap A$  is non-empty  
 This contradicts that  $Y \cap A = \phi$   
 So,  $X = Y$
12. (d) (a)  $x \in A - B \Leftrightarrow x \in A$  and  $x \notin B$   
 $\Leftrightarrow x \in A$  and  $x \in B'$   $\Leftrightarrow x \in A \cap B'$   
 $\therefore A - B = A \cap B'$  ... (i)  
 $x \in A$  and  $x \in B'$   
 $\Leftrightarrow x \notin A'$  and  $x \in B' \Leftrightarrow x \in B'$  and  $x \notin A'$   
 $\Leftrightarrow x \in B' - A'$